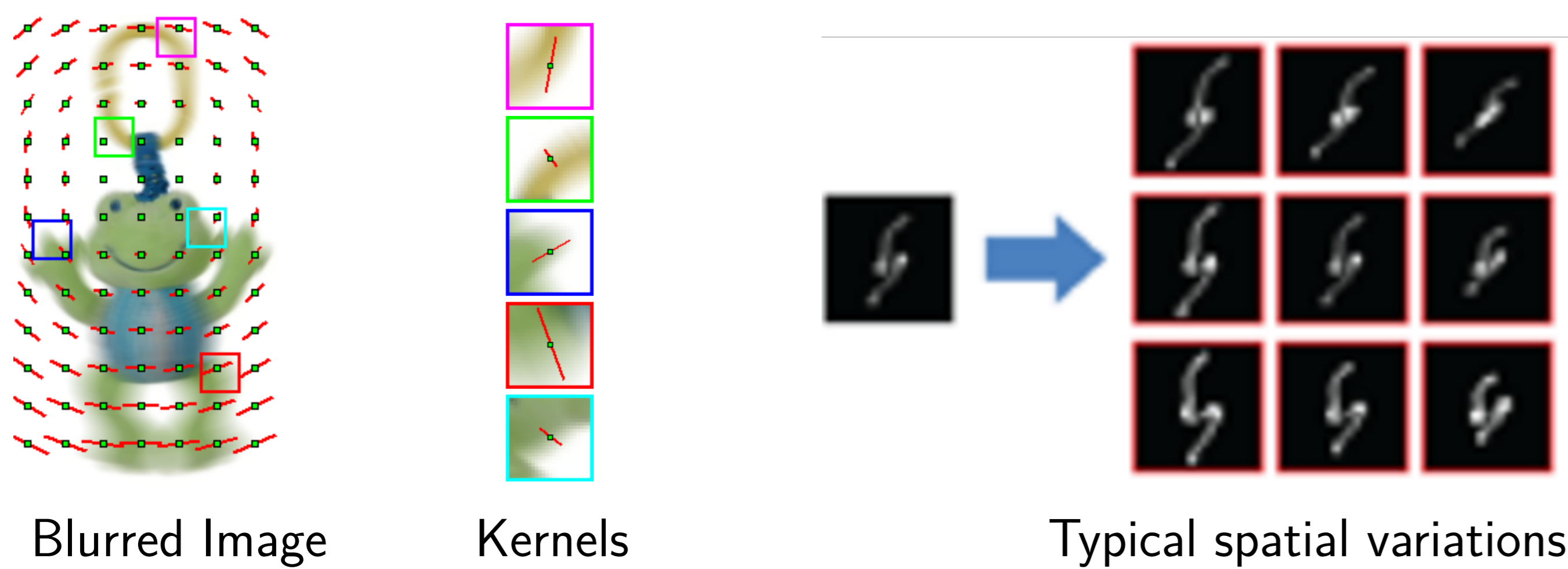


## Introduction and motivation

- Given a single image of a static 3D scene, this work solves two tasks: a **Exposing Image Forgery** and a **Depth-based Scene Segmentation** by recovering camera motion that occurred during exposure.
- Necessary, since it is not possible to detect using naked eye. Previous techniques could not handle 3D scenes containing motion blur.
- High level idea:** Scene Depth, camera trajectory and motion-blur kernels are inter-related.
- Challenge:** Knowledge of one is required to estimate the other.
- Solution:** Discovered a consistency between horizontal and vertical projections of spatially-varying blur kernels within an image.



## Blurring Model

- Pixel correspondences  $\mathbf{x}$  and  $\mathbf{x}_\lambda$  at depth  $Z$ , after a transformation  $[\phi^\lambda, T^\lambda]$

$$\mathbf{x}_\lambda = KR_\lambda K^{-1}\mathbf{x} + \frac{KT_\lambda}{Z} \quad (1) \quad \mathbf{x}_\lambda = P_{\phi^\lambda, T^\lambda}(\mathbf{x}) = \begin{pmatrix} 1 - \phi_z^\lambda & f & t_x^\lambda \\ \phi_z^\lambda & 1 & f & t_y^\lambda \\ 0 & 0 & 1 & Z \end{pmatrix} \mathbf{x}$$

- If  $w_i$  denotes the fraction of time camera spent in position  $i$ , motion blurred image  $B$  can be derived from focussed image  $I$  as

$$B(\mathbf{x}) = \sum_{i=1}^N w_i I(P_{\phi_i, T_i}^{-1}(\mathbf{x})) \quad (2)$$

- Similarly, PSF at  $\mathbf{x} = (x, y)$  can be derived from a single point:

$$p(x, y) = \sum_{i=1}^N w_i \delta(P_{\phi_i, T_i}^{-1}(x, y)) \quad (3)$$

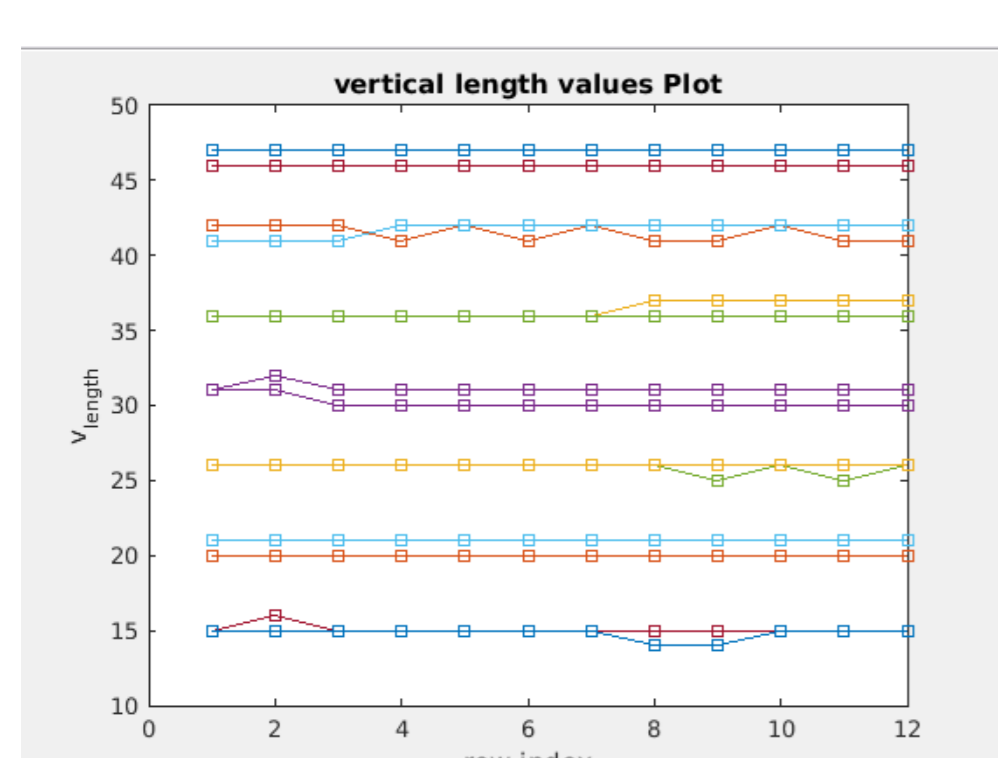
- In matrix form, it is equivalent to  $p^{(x,y)} = M^{(x,y)} W_D$

## Consistency of $h_{\text{length}}$ and $v_{\text{length}}$

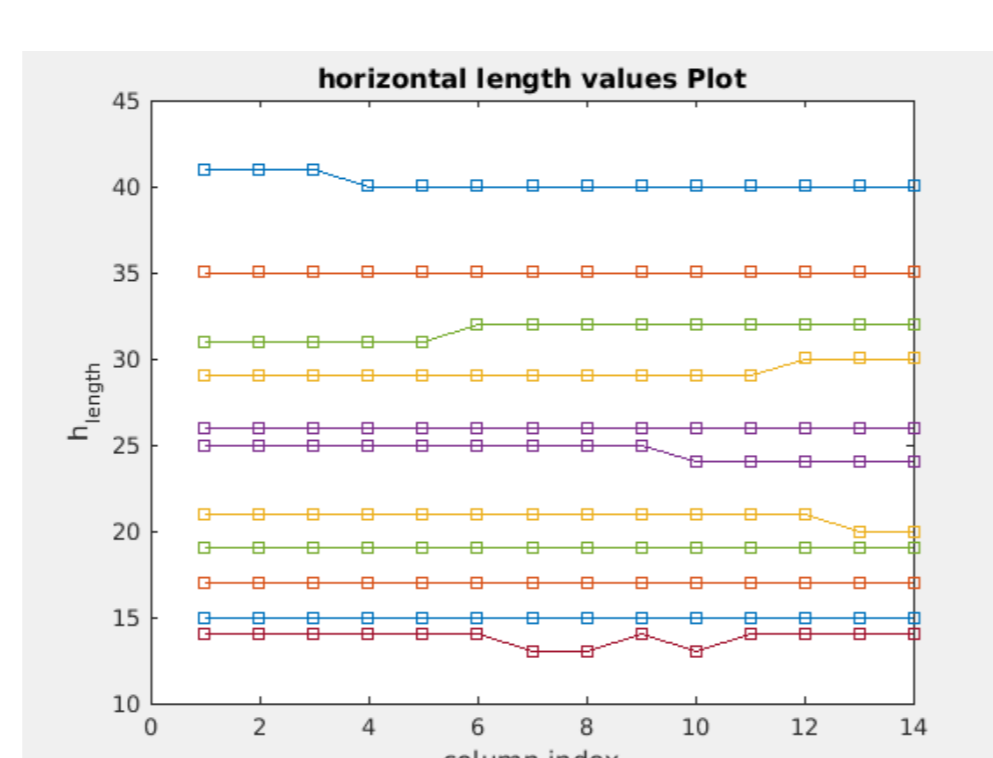
- Assumption** Small angle of rotation  $\phi$ .
- If we pick any two points:  $\mathbf{x}_i$  and  $\mathbf{x}_j$  on a PSF, the difference in their spatial locations can be expressed in terms of the PSF's pixel coordinate  $x$  and  $y$ :

$$\Delta x_{ij}^l = (x^l \ y^l \ 1) \begin{pmatrix} 0 \\ -(\phi^j - \phi^i) \\ (t_x^j - t_x^i)f \\ Z^l \end{pmatrix} = -y^l (\Delta \phi^{ij}) + \frac{(\Delta t_x^{ij})f}{Z^l} \quad (4)$$

$$\Delta y_{ij}^l = (x^l \ y^l \ 1) \begin{pmatrix} (\phi^j - \phi^i) \\ 0 \\ (t_y^j - t_y^i)f \\ Z^l \end{pmatrix} = x^l (\Delta \phi^{ij}) + \frac{(\Delta t_y^{ij})f}{Z^l} \quad (5)$$



(a) Vertical-lengths vs rows



(b) Horizontal-lengths vs columns

Figure 1: We can see that values  $\Delta x_{ij}^l$  and  $\Delta y_{ij}^l$  turn out to be constant for all the PSFs lying on same column index  $y$  and same row index  $x$ , respectively.

## Camera Trajectory Estimation

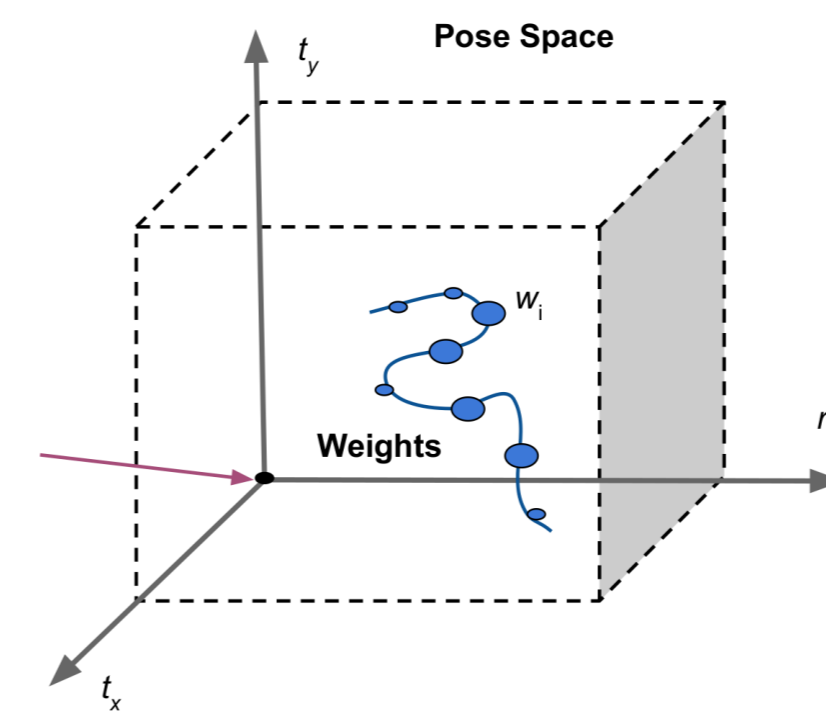


Figure 2: Camera Trajectory.

- Camera Trajectory estimation from local PSFs. Algorithm: [3].

$$p^{\text{set}} = M^{\text{set}} W_D \quad (6)$$

- Minimize with sparsity constraint.

$$\| p^{\text{set}} - M^{\text{set}} W_D \|^2 + c \| W_D \|^1 \quad (7)$$

## Matching PSFs at various depths

Using depth and camera trajectory, we generate all possible PSFs at location  $\mathbf{x}$ . If the pixel  $\mathbf{x}$  was actually situated at a different scene depth  $D_i$ , the PSF would be modified as follows

$$p^{D_i}(\mathbf{x}, \mathbf{a}) = \sum_{\lambda=1}^N w_\lambda \delta(\mathbf{a} - (P_{\phi^\lambda, T^\lambda}(\mathbf{x}) - \mathbf{x})) d\tau \quad (8)$$

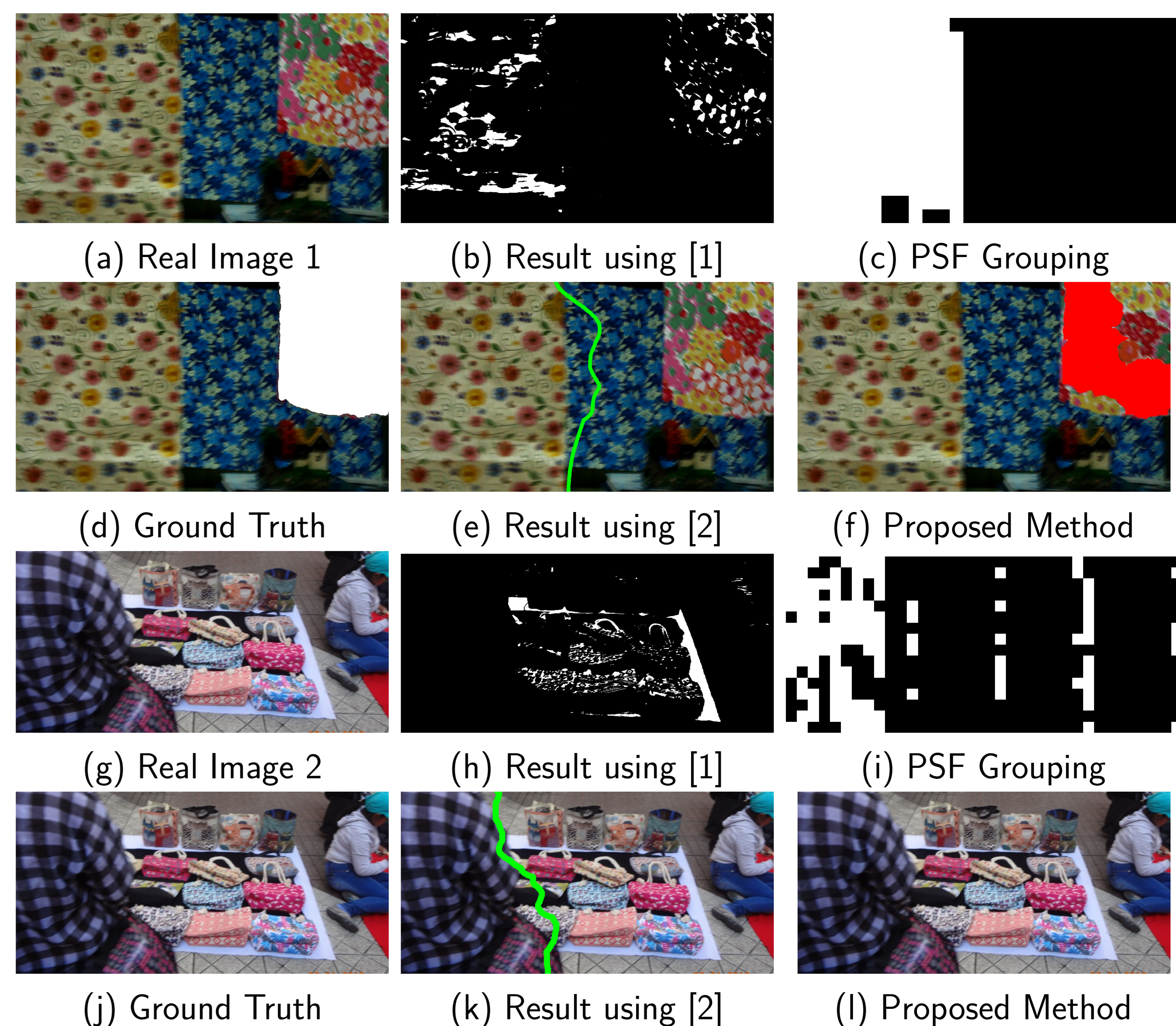
Low cross-correlation between actual PSF and estimated PSFs  $\rightarrow$  Region Spliced!

## Results

- Finally, we utilize natural image texture segmentation [Mobahi, IJCV 2011] of the input image to obtain meaningful region boundaries.



Table 1: Intermediate results after each step (a) Input spliced image (b) PSF grouping (all white pixels belong to single depth layer) (c) Patch-wise inconsistency between blur kernels (d) Texture based segmentation of the input image (e) Final result showing localized spliced region in red



## References

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- M. P. Rao, A. N. Rajagopalan, and G. Seetharaman, "Harnessing motion blur to unveil splicing," vol. 9, no. 4. IEEE, 2014, pp. 583–595.
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